## MHF4U Unit 5 Trigonometry

| Section | Pages | Questions |
| :---: | :---: | :--- |
| Prereq Skills | $250-251$ | \#1ac, 2ac, 3ace, 4ace, 5, 6, 8(graph the function), 9(graph the function), 10, <br> 11, 12ab, 15 |
| 5.1 | $258-259$ | \#1ad, 2ad, 3ad, 4ad, 5bc, 6bc, 7ab, 8ab, 9, 10, 11, 12, 17 |
| 5.2 | $275-279$ | \#1abce, 2, 3, 4, 5(don't graph), 6(don’t graph), 8ab, 9ab, 10, 11, 12a, 13a, 19a |
| 5.3 | $267-269$ | \#7, 9a, 10, 13, 15*, 16*, 18 |
| 5.4 | $287-289$ | \#1abe, 3ab, 5be, 7cd, 9, 10, 11, 12, 13bc, 14, 16, 17, 18, 19, 20, 22*, 26 |
| 5.5 | $296-299$ | \#1, 3, 4abef, 6, 10, 11ab, 12 |
| Review | $300-301$ <br> $302-303$ | \#1, 2, 3, 4, 6a, 7, 8, 9, 10, 11, 12 <br> \#2-7, 9-15 |

Note: Questions with an asterisk* are extra questions that are optional for the daily homework. However, they are potential "extended-type" questions that could be included on a unit test.

Graph of $y=\sin x$ for $-360^{\circ} \leq x \leq 360^{\circ}$.

| $x$ | $y$ |
| :---: | :---: |
| $-360^{\circ}$ | 0 |
| $-270^{\circ}$ | 1 |
| $-180^{\circ}$ | 0 |
| $-90^{\circ}$ | -1 |
| $0^{\circ}$ | 0 |
| $90^{\circ}$ | 1 |
| $180^{\circ}$ | 0 |
| $270^{\circ}$ | -1 |
| $360^{\circ}$ | 0 |

## Key Features



Period $=360^{\circ}$,
Max for $\mathrm{y}=1$,
Min for $y=-1$
Amplitude $=1$,
Phase Shift $=0^{\circ}$
Vertical Displacement $=0$
x-intercepts: $-360^{\circ},-180^{\circ}, 0^{\circ}, 180^{\circ}, 360^{\circ}$
y-intercept: 0
Domain: $\left\{x \in R \mid-360^{\circ} \leq x \leq 360^{\circ}\right\}$
Range: $\{y \in R \mid-1 \leq y \leq 1\}$

Graph of $y=\cos x$ for $-360^{\circ} \leq \mathrm{x} \leq 360^{\circ}$.

| $x$ | $y$ |
| :---: | :---: |
| $-360^{\circ}$ |  |
| $-270^{\circ}$ |  |
| $-180^{\circ}$ |  |
| $-90^{\circ}$ |  |
| $0^{\circ}$ |  |
| $90^{\circ}$ |  |
| $180^{\circ}$ |  |
| $270^{\circ}$ |  |
| $360^{\circ}$ |  |



Period $=$
Max for $\mathrm{y}=$
Min for $\mathrm{y}=$

Amplitude $=$
Phase Shift =
Vertical Displacement $=$
x -intercepts:
$y$-intercept:
Domain:
Range:

## Transformations of Sinusoidal Functions

$y=a \sin (k(\theta-d))+c$

$$
y=a \cos (k(\theta-d))+c
$$

$\mathrm{a}=$ amplitude (vertical stretch or compression)
$\mathrm{k}=$ horizontal stretch or compression
$\mathrm{d}=$ phase shift (horizontal translation)
$\mathrm{c}=$ vertical displacement (vertical translation)
Period $=360 \% \mathrm{k}$ (time needed to complete one cycle or wavelength)
Frequency $=1 /$ Period (number of cycles per unit of time)

Example: Describe the transformations that must be applied to the graph of $f(x)=\sin x$ to obtain the graph $g(x)=-0.5 \sin \left[3\left(x+150^{\circ}\right)\right]+3$. Graph the functions $f(x)$ and $g(x)$ on the same grid and state the domain and range.


Example: Describe the transformations that must be applied to the graph of $f(x)=\cos x$ to obtain the graph $g(x)=2 \cos \left[2\left(x-120^{\circ}\right)\right]-2$. Graph the functions $f(x)$ and $g(x)$ and state the domain and range.


Graph of $y=\tan x$ for $-360^{\circ} \leq \mathrm{x} \leq 360^{\circ}$.

| $x$ | $y$ |
| :---: | :---: |
| $-360^{\circ}$ |  |
| $-315^{\circ}$ |  |
| $-270^{\circ}$ |  |
| $-225^{\circ}$ |  |
| $-180^{\circ}$ |  |
| $-135^{\circ}$ |  |
| $-90^{\circ}$ |  |
| $-45^{\circ}$ |  |
| $0^{\circ}$ |  |
| $45^{\circ}$ |  |
| $90^{\circ}$ |  |
| $135^{\circ}$ |  |
| $180^{\circ}$ |  |
| $225^{\circ}$ |  |
| $270^{\circ}$ |  |
| $315^{\circ}$ |  |
| $360^{\circ}$ |  |



## Key Features

Period $=$

Max for $\mathrm{y}=$
Min for $\mathrm{y}=$

Amplitude $=$
Phase Shift =
Vertical Displacement $=$
x-intercepts:
$y$-intercept:
Domain:
Range:

